Please write legibly and show all work. If the answer to a problem is written down correctly, but certain steps of solving it are not shown, points might be taken off.

1. Consider the following matrices.

$$A = \begin{bmatrix} 3 & -1 \\ 2 & 1 \\ 1 & 4 \end{bmatrix}, \quad B = \begin{bmatrix} -2 & 3 & 1 \\ 4 & -1 & 1 \end{bmatrix}, \quad C = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 2 & 3 & 0 \end{bmatrix}, \quad E = \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix}$$

Compute the following expressions.

- (a) AB + I. (Here I is the  $3 \times 3$  identity matrix.)
- (b) BC 2B.
- (c) CE + 3E.
- 2. Find all eigenvalues and all eigenvectors for the following matrices.

(a) 
$$\begin{bmatrix} 6 & -7 \\ 1 & -2 \end{bmatrix}$$
 (b)  $\begin{bmatrix} 4 & 1 & 4 \\ 1 & 7 & 1 \\ 4 & 1 & 4 \end{bmatrix}$  (c)  $\begin{bmatrix} 3 & -1 \\ 1 & 1 \end{bmatrix}$ 

For the next problems: (a) find the general solution to the given system of differential equations, and (b) draw the corresponding phase portrait.

- 3.  $x'_1 = 6x_1 7x_2, x'_2 = x_1 2x_2.$
- 4. x' = -y, y' = 4x.
- 5.  $x'_1 = 9x_1 + 5x_2, x'_2 = -6x_1 2x_2.$
- 6. x' = x 2y, y' = 2x + y.