

Math 311 — Final Overview.

The following areas may be on the final:

- (1) First order differential equations
  - (a) Existence and Uniqueness
  - (b) Slopefields, solution curves
  - (c) Solving 1st order equations: separable, linear, substitution
  - (d) autonomous equations, phase plots
  - (e) population models: natural, logistics, with harvesting
  - (f) acceleration-velocity models
- (2) Higher order linear equations
  - (a) Existence and Uniqueness
  - (b) General solutions
  - (c) linear equations with constant coefficients, homogeneous and non-homogeneous
  - (d) spring models
- (3) 2D Systems of Differential Equations
  - (a) Solve  $\mathbf{x}' = A\mathbf{x}$  where  $A$  is a  $2 \times 2$  real matrix.
  - (b) conversion between a 2nd order equation and a system of 1st order equations
  - (c) Sketch phase portraits of these systems.
- (4) Laplace Transforms
  - (a) Calculate Laplace Transform of  $f$  from definition
  - (b) Use Table of basic Laplace Transforms and combination rules (including partial fractions) to compute Laplace Transform.
  - (c) Solve differential equations using a Laplace Transform.

The following will not be covered: Exact Equations, Numerical Methods, Non-linear systems, Laplace Transform of Periodic Functions.