

**J. Raphson**

*Analysis Aequationum universalis*, London, 2nd ed., 1697, pp. 8 and 20.

PROP. II

Let it be proposed that  $ba - aaa = c$

Let there be chosen any quantity whatever ( $g$ ) less than ( $a$ ). I say that ( $g$ ) obtained closer and closer (by our method), being always greater than its predecessor, but certainly less than ( $a$ ), will therefore converge to the true value.

By this hypothesis,  $g + z = a$ . So,

$$bg - ggg + b - 3gg \times z - 3gzz - zzz = ba - aaa = c$$

Therefore  $b - 3gg \times z - 3gzz - zzz = c + ggg - bg$

Therefore  $+z - \frac{3gzz + zzz}{b - 3gg} = \frac{c + ggg - bg}{b - 3gg} = +x$ .

From the convergence Theorems, we have  $+z = +x + \frac{3gzz + zzz}{b - 3gg}$ ,

and adding ( $g$ ) to both parts, produces

$$g + z = a = g + x + \frac{3gzz + zzz}{b - 3gg}$$

But this new ( $g$ ) =  $g + x$  is greater than the preceding, by the quantity ( $x$ ), and less however than ( $a$ ), by the quantity  $\frac{3gzz + zzz}{b - 3gg}$ , part of its total. Q.E.D.[...]

PROBLEM XII

Trisection of the angle

Given the Radius of a Circle =  $r$  and the Chord of an arc =  $c$ , what is the Chord of the Third part of the arc?

The equation  $3rra - aaa = crr$  will give the Chord of an arc of 20 degrees, the Third part of sixty.

In the case  $c = r = 10.000$  and the equation being  $300a - aaa = 1000$ , (namely)  $ba - aaa = c$ , then according to the preceding theorem:

$$\begin{array}{r} g = 3 \\ c + ggg - bg = + 127 \\ b - 3gg = + 273 \end{array} \quad \frac{+ 1270}{+ 273} \quad (+.4 = x$$

$$\frac{3.}{+ .4}$$

$$\begin{array}{r} g = 3.4 \\ c + ggg - bg = + 19.304 \\ b - 3gg = 265.32 \end{array} \quad \frac{+ 19.3040}{+ 265.32} \quad (+.072 = x$$

$$\frac{3.4}{+ .072}$$

$$g = 3.472$$

$$\begin{array}{r} c + ggg - bg = + 254210048 \\ b - 3gg = 263.835648 \end{array} \quad \frac{+ 2542100480}{+ 263.835648} \quad (+.0009636 = x$$

$$\frac{3.472}{+ .0009636}$$

$$g = 3.4729636$$

$$\begin{array}{r} c + ggg - bg = - .0000123100024899 \\ b - 3gg = 263.8155715 \end{array} \quad \frac{- .0000123100024899}{- .0000123100024899} \quad (-.0000046661393 = x$$

$$\frac{3.4729636}{- .0000046661393}$$

$$a = 3.472963553338602$$